

## SPECTROSCOPIC DIAGNOSTICS OF HIGH CURRENT DENSITY EXPLODING COPPER WIRE PLASMA AT STANDARD AMBIENT TEMPERATURE PRESSURE

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### ABSTRACT

Optical emission spectroscopy was applied to study electron temperature and electron number density of plasma generated during exploding copper wires. Neutral spectral lines dominated spectrum in visible range which are used for determination of electron temperature and electron number density. Transitions  $3d^9 4s(^3D)5s^2 D_{3/2} \rightarrow 3d^9(^2D)4s4p(^3P^0)^2 F^0_{5/2}$  at 464.25 nm,  $3d^{10} 4p^2 P^0_{3/2} \rightarrow 3d^9 4s^2 D_{5/2}$  at 510.55 nm,  $3d^{10} 4d^2 D_{3/2} \rightarrow 3d^{10} 4p^2 P^0_{1/2}$  at 515.32 nm,  $3d^{10} 4d^2 D_{5/2} \rightarrow 3d^{10} 4p^2 P^0_{3/2}$  at 521.82 nm and  $3d^{10} 4p^2 P^0_{3/2} \rightarrow 3d^9 4s^2 D_{3/2}$  at 570.02 nm are used for determination of electron temperature using Boltzmann plot method. Electron number density is determined by using Stark broadened 521.82 nm Cu I line. Electron temperature and electron number density is found to be in range 9200 K to 18200 K and  $3.02 \times 10^{16} \text{ cm}^{-3}$  to  $6.91 \times 10^{16} \text{ cm}^{-3}$ . Variation of electron temperature and electron number density is studied as function of wire cross section area and discharge energy. Plasma parameters are observed to vary directly with discharge energy and inversely with cross section area of wire being exploded. Validity of assumption of local thermodynamic equilibrium is also discussed.

**KEYWORDS:** Electron Temperature, Electron Number & Local Thermodynamic Equilibrium

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### INTRODUCTION

The phenomena associated with exploding wires are investigated for a variety. Literature is not abundant in its depth but there are a several groupings of papers, theoretical[1-3], purely experimental[4, 5] and combination of these two[6]. It is common to find exploding wire cited for Pressure vessel testing[7], method of propulsion[8], controlled ignition system for solid fuelled ammunitions[9], ignition system for confined fusion research[4], thin film production[10], generation of blast wave[11] and production of high purity metallic and alloy nanoparticles[10, 12].

First observation of exploding wires was reported back to Nairne's experiment in 1780[13]. During early 20th century research into exploding wires increased due to military interest. It was found that the mechanisms were highly dependent upon local experimental conditions, furthermore slight differences hindered absolute repeatability of the experiments[14]. Crystal size, orientation of metal wire, orientation of cold pre-drawn metal wire, pressure surrounding metal wire, circuit differences and initial temperature differences are the reasons behind

differences in repeated experimentation[15]. Instantaneous current densities during wire explosion depend on type of experimental arrangement and generally are in range of  $10^7$  to  $10^9$  A/cm<sup>2</sup> [16-18]. Plasma parameters, plasma properties, plume dynamics and effects of laser parameters of laser induced plasmas have been studied extensively using various theoretical models and experiments results [19-23]. Laser induced copper plasma has been extensively studied using Excimer and Nd:YAG lasers[24-26].

Present work reports the study of exploding copper wire plasma in air, carried out by high current density copper wire explosions in air using capacitor bank. Optical emission spectroscopy of exploding wire plasma was recorded to determine electron temperature and electron number density at different discharge energies for wires of different cross sectional area. In our knowledge this is first report on controlling exploding wire plasma parameters by discharge energy and wire thickness.

## EXPERIMENTAL DETAILS

4x4 capacitor bank of total capacitance 10  $\mu$ F rated at 1800 V was used to give high current density discharge in thin copper wire causing it to explode. Cylindrical copper wires of length 3 cm were exploded for each experiment in a glass tube of typical commercially used electric fuse shape glass cylinder with internal and external diameter of 3 mm and 5 mm respectively. Capacitor bank was constructed by connecting 10  $\mu$ F, 450 V capacitors with 15mm x 6mm aluminum strips, which was further connected with 3AWG (5.827 mm diameter) copper wire with rated current of 100 A (fuse current of 8.1 kA for 1s and 45 kA for 32 ms) at 38°C. The glass tube was mounted on a fixed stage and radiation from plasma was collected by fiber optics (600  $\mu$ m core diameter) having a collimating lens with 45° field of view, placed on perpendicular bisector of glass tube at 3.62 cm from glass tube in order to collect all the light produced during explosion. Optical fiber was connected with PC2000 spectrometer (Ocean Optics Inc.) having slit width 25  $\mu$ m is equipped with 2048 elements CCD array to record optical emission. Spectrum was recorded in range from 350 nm to 850 nm with a resolution of 0.36 nm. Temporal window was set at 100 $\mu$ s delay which was sufficient enough for plasma to be assumed in local thermodynamic equilibrium. Average of five sets of electron temperature and electron number density was taken under same experimental condition.

## RESULTS AND DISCUSSIONS

### Optical Emission Spectra

Exploding copper wire plasma generated in air by large current pulse expands in a cylindrical pattern away from exploded wire towards inner surface of glass tube due to shockwave [7]. In the present work copper spectra were recorded for different discharge voltage across copper wire from 400 V to 1600 V in 200 V steps having discharge energy ranging from 0.8 J to 12.8 J. Plasma emission was registered as a function of cross-sectional area of exploded wire with diameters 89.7  $\mu$ m, 127  $\mu$ m, 160  $\mu$ m, 227  $\mu$ m, 286  $\mu$ m, 321  $\mu$ m and 361  $\mu$ m. Figure 1 shows the plasma emission spectrum of copper generated by applying 1000 V across 89.7  $\mu$ m thick copper wire covering range of 350-850 nm. Dominating lines belong to emission of neutral copper, with strongest being observed at 406.24, 464.25, 510.55, 515.32, 521.82, 529.25, 570.02, 578.21, 793.31 and 809.26 nm corresponding to transitions shown in table 1 based on data listed in tables of National Institute of Standards and Technology (NIST)[27].

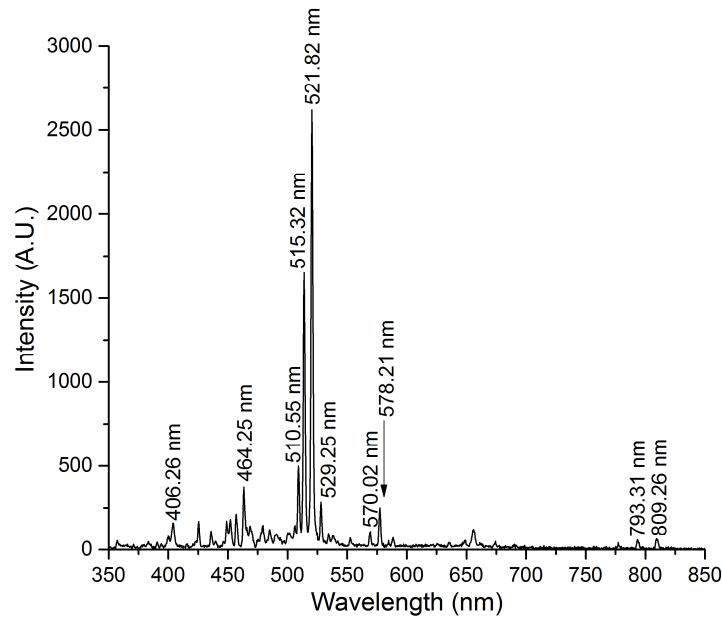


Figure 1: Emission Spectrum of Copper Plasma Generated by Exploding 89.7  $\mu\text{m}$  Diameter Copper Wire at 1000 V Showing Neutral Copper Spectral Lines

Table 1: Spectroscopic Parameters of Cu(I) Lines

Wavelength (nm)	Transitions	Upper Level Statistical Weight (g)	Transition Probabilities ( $10^8 \text{ s}^{-1}$ ) (A)	Excitation Energy (eV) ( $E_n$ )
406.26	$3d^{10}5d^2D_{5/2} \rightarrow 3d^{10}4p^2P^0_{3/2}$	6	1.26	6.94683
464.25	$3d^9 4s(^3D) 5s^2D_{3/2} \rightarrow 3d^9(^2D) 4s4p(^3P^0)^2F^0_{5/2}$	4	0.074	8.09122
510.55	$3d^{10} 4p^2P^0_{3/2} \rightarrow 3d^9 4s^2D_{5/2}$	4	0.02	3.81669
515.32	$3d^{10} 4d^2D_{3/2} \rightarrow 3d^{10} 4p^2P^0_{1/2}$	4	0.6	6.19117
521.82	$3d^{10} 4d^2D_{5/2} \rightarrow 3d^{10} 4p^2P^0_{3/2}$	6	0.75	6.19203
529.25	$3d^9 4s(^3D) 5s^4D_{7/2} \rightarrow 3d^9(^2D) 4s4p(^3P^0)^4D^0_{7/2}$	8	0.109	7.73703
570.02	$3d^{10} 4p^2P^0_{3/2} \rightarrow 3d^9 4s^2D_{3/2}$	4	0.0028	3.81669
578.21	$3d^{10} 4p^2P^0_{1/2} \rightarrow 3d^9 4s^2D_{3/2}$	4	0.0028	3.81669
793.31	$3d^{10} 5s^2S_{1/2} \rightarrow 3d^{10} 4p^2P^0_{1/2}$	2	- <sup>a</sup>	5.34833
809.26	$3d^{10} 5s^2S_{1/2} \rightarrow 3d^{10} 4p^2P^0_{3/2}$	2	- <sup>a</sup>	5.34833

<sup>a</sup> Transition probabilities not yet reported in literature

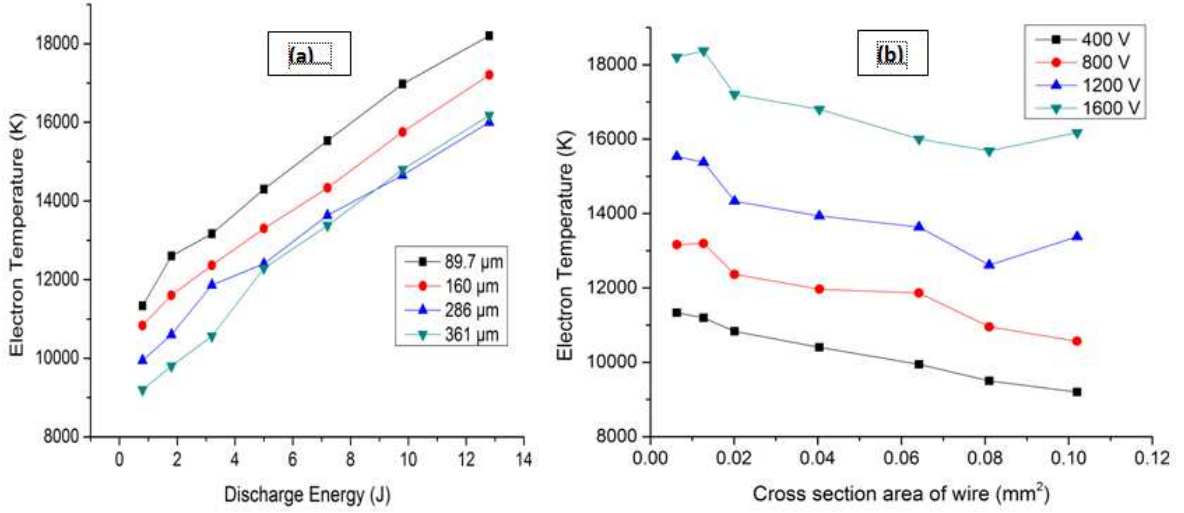
## Electron Temperature

Electron temperature was determined using Boltzmann plot method by assuming the plasma in local thermodynamic equilibrium (LTE) [28-30] using:

$$\ln \left( \frac{I_{nk} \lambda_{nk}}{A_{nk} g_n} \right)_i = a - \frac{E_i}{kT} \quad (1)$$

where  $I_{nk}$  is integrated line intensity of transition involving upper level ( $n$ ) to lower level ( $k$ ),  $\lambda_{nk}$  is wavelength associated with the transition,  $A_{nk}$  is the transition probability,  $g_n$  is upper level ( $n$ ) statistical weight,  $E_n$  is energy of upper level ( $n$ ),  $a$  is ratio of total number density and partition function which remains constant,  $k$  is Boltzmann constant and  $T$  is excitation temperature. Boltzmann plot between  $\ln(I\lambda/gA)$  and upper level energy  $E_n$  whose slope equals  $(-1/kT)$  gives electron temperature. Error originating from uncertainty in transition probabilities and integrated intensities is determined to be  $\approx 10\%$ . Line identification and different spectroscopic parameters such as wavelength( $\lambda$ ), transition levels, transition

probabilities ( $A$ ), statistical weight ( $g$ ) and upper level energy listed in table 1 are taken from NIST atomic spectroscopy database[27]. For determination of electron temperature neutral copper lines at 464.25 nm, 510.55 nm, 515.32 nm, 521.82 nm and 570.02 nm were used.



**Figure 2: (a) Variation of Electron Temperature with Discharge Energy for Explosion for Wires of Diameter 89.7 μm, 160 μm, 286 μm and 361 μm. (b) Variation of Electron Temperature with Cross Sectional Area of Wire at 400, 800, 1200 and 1600 V**

Behavior of electron temperature was studied as function of energy provided for wire explosion and thickness of wire being exploded. It was observed that electron temperature varied from 9893 K to 17205 K for 400 to 1600 volts with 0.8 J to 12.8 J discharge energy for 160 μm diameter wires, same experiment was repeated for wires of diameter 89.7 μm, 127 μm, 227 μm, 286 μm, 321 μm and 361 μm. Behavior of electron temperature with applied voltage and discharge energy at wires of diameter 89.7 μm, 160 μm, 286 μm and 361 μm is shown in Figure 2(a). It is evident that electron temperature increases with applied voltage which obviously is due to increase in discharge energy provided by capacitor bank. Behavior of electron temperature varies as square of the applied voltage and almost linearly with the discharge energy. It can also be seen that electron temperature drops as the wire thickness increases. Figure 2(b) shows the behavior of electron temperature with cross sectional area of the wire at 400 V, 800 V, 1200 V and 1600 V, which clearly indicates that electron temperature decreases almost linearly by increasing cross sectional area of wire being exploded which indicates direct dependence of electron temperature on current density in the wire during explosion.

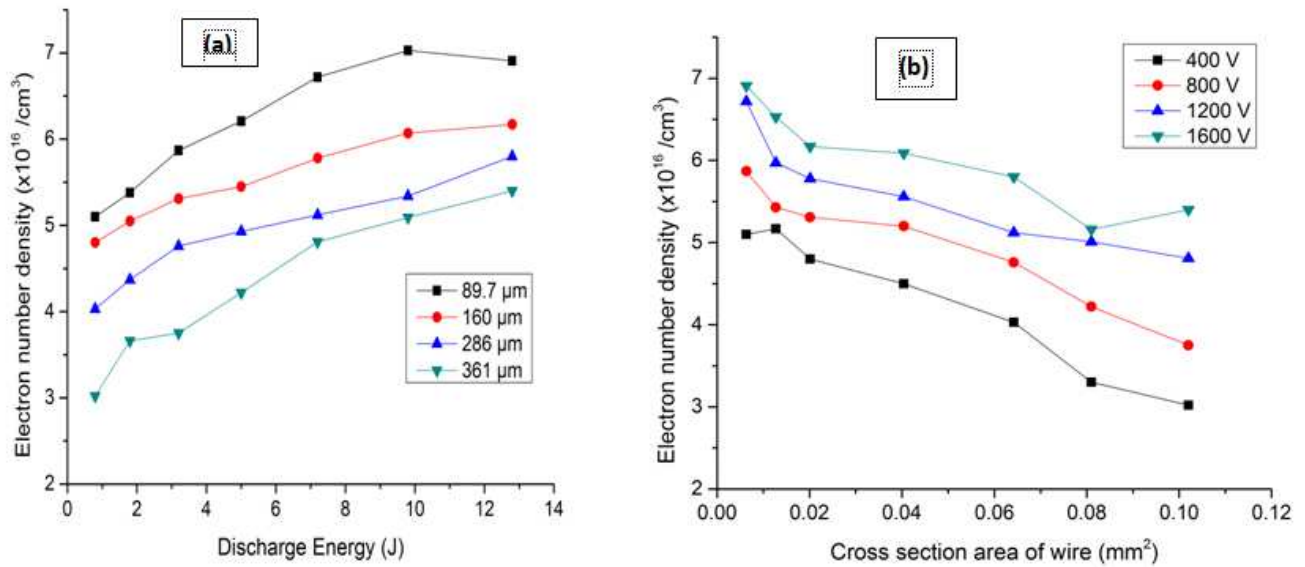
### Electron Number Density

Main sources of line broadening are Doppler broadening, ion-impact broadening and Stark broadening. Since the plasma is initially in free expansion state [31], contribution of ion-impact broadening is neglected. The estimated Doppler's width for Cu (I) line at 521.2 nm is 0.00297 nm, corresponding to a 10000 K plasma temperature, and observed line width is around 1.8 nm. Since Doppler broadening contribution is negligibly smaller than observed line width, major contribution is attributed to Stark broadening. Electron number density ( $N_e$ ) related to full width at half maximum (FWHM) of Stark broadened lines is given by the estimation of the FWHM ( $\Delta\lambda_{1/2}$ ) for neutral atoms as[32-34]:

$$\Delta\lambda_{1/2} = 2\omega \left( \frac{N_e}{10^{16}} \right) + 3.5A \left( \frac{N_e}{10^{16}} \right)^{1/4} \left[ 1 - \frac{3}{4} N_d^{-1/3} \right] \left( \frac{N_e}{10^{16}} \right) \quad \dots \quad (2)$$

Where  $\omega$  represents electron impact width parameter,  $A$  is ion broadening parameter,  $N_e$  is electron number density and  $N_d$  is number of particles in Debye sphere. First term refers to broadening due to the electron contribution, whereas second term is attributed to ion broadening. Since contribution of ionic broadening is usually very small, it can be neglected [35, 36] and above equation reduces to a simpler form:

$$\Delta\lambda_{1/2} = 2\omega \left( \frac{N_e}{10^{16}} \right) \quad \dots \quad (3)$$



**Figure 3: (a) Variation of Electron Number Density with Discharge Energy for Explosion for Wires of Diameter 89.7  $\mu\text{m}$ , 160  $\mu\text{m}$ , 286  $\mu\text{m}$  and 361  $\mu\text{m}$ , (b) Variation of Electron Number Density with Cross Sectional Area of Wire at 400, 800, 1200 and 1600 V**

Electron number density of the plasma was determined by using strongest observed neutral copper line at 521.82 nm fitted with Voigt profile, value of electron impact width parameter corresponding to different plasma temperatures is taken from the reference data tabulated by Konjevic and Wiese[37].

The behavior of electron number density was studied as a function of discharge energy provided for wire explosion and cross sectional area of wire being exploded. It was observed that electron number density varied from  $4.8 \times 10^{16} \text{cm}^{-3}$  to  $6.17 \times 10^{16} \text{cm}^{-3}$  for 400 to 1600 volts having discharge energy from 0.8 to 12.8 J for 160  $\mu\text{m}$  diameter copper wire. Same experiment was repeated for wires of diameter 89.7  $\mu\text{m}$ , 127  $\mu\text{m}$ , 227  $\mu\text{m}$ , 286  $\mu\text{m}$ , 321  $\mu\text{m}$  and 361  $\mu\text{m}$ . Behavior of electron number density with discharge energy at wires of diameter 89.7  $\mu\text{m}$ , 160  $\mu\text{m}$ , 286  $\mu\text{m}$  and 361  $\mu\text{m}$  is shown in figure 3(a). It is evident that electron number density increases with increase in discharge energy provided by the capacitor bank. Figure 3(b) shows the behavior of electron number density with cross sectional area of the wire at 400 V, 800 V, 1200 V and 1600 V, which clearly indicates that electron number density decreases by increasing the cross sectional area of wire being exploded showing direct dependence of electron number density on current density in the wire during explosion.

#### **Validity of Assumption of Local Thermodynamic Equilibrium**

Optically thick plasmas do not give meaningful values of the plasma parameters, for determination of electron temperature and electron number density optically thin plasma is necessary. During the early stages of explosion, plasma is

observed to be optically thin. Optically thick plasmas would have self-absorption where strong lines would have dips at the central wavelengths, however in spectra used for present calculations, no dips at central wavelength of observed lines were found. The condition of LTE that the atomic and ionic states should be populated and depopulated predominantly by electron collisions, rather than by radiation, requires an electron density which is sufficient to ensure the high collision rate. Validity of the assumption of LTE is confirmed by McWhirter's criterion [38, 39], which conditions the minimum electron number density.

$$N_e \geq 1.6 \times 10^{12} T^{1/2} \Delta E^3 \quad \dots \quad (4)$$

Where T (K) is the plasma temperature and  $\Delta E$  (eV) is the energy difference between the states which are expected to be in local thermodynamic equilibrium (LTE). At temperature 14000 K and states corresponding to copper line at 521.82 nm, equation (4) yields  $N_e \approx 2 \times 10^{15} \text{ cm}^{-3}$ , which defines the validity of LTE plasma in the present work.

## CONCLUSIONS

We have studied exploding copper wires for plasma parameters. Emission spectrum in visible region shows transition of neutral copper in plasma. Electron temperature and electron number density has been determined as a function of discharge energy and cross section area of the wire being exploded. It was observed that the electron temperature and electron number density increases with discharge energy and vice versa. Variation of electron temperature and electron number density with diameter of wire being exploded shows the direct relation of these parameters with the current density in the wire as both decrease with increasing cross section area of wire. Plasma parameters reported in this work are of same order of magnitude as previously reported in literature for other plasma generation techniques [19, 24, 26]. We show that plasma parameters can be controlled with good accuracy by variation of discharge energy and cross sectional area of wire being exploded.

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